## Sense Making: Is it at the Core of Your Classroom?

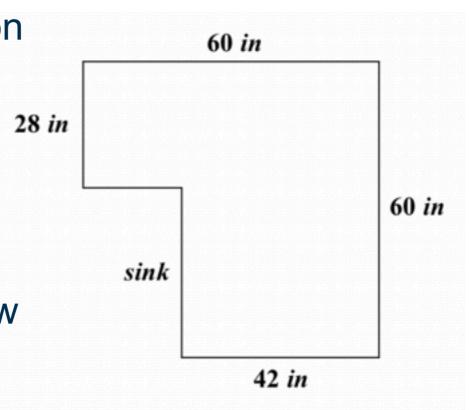


Annie Fetter
anniefetter@gmail.com
@MFAnnie
#PCTM19

Slides and links to related resources will be available on my blog after the talk: annie.mathematicalthinking.org

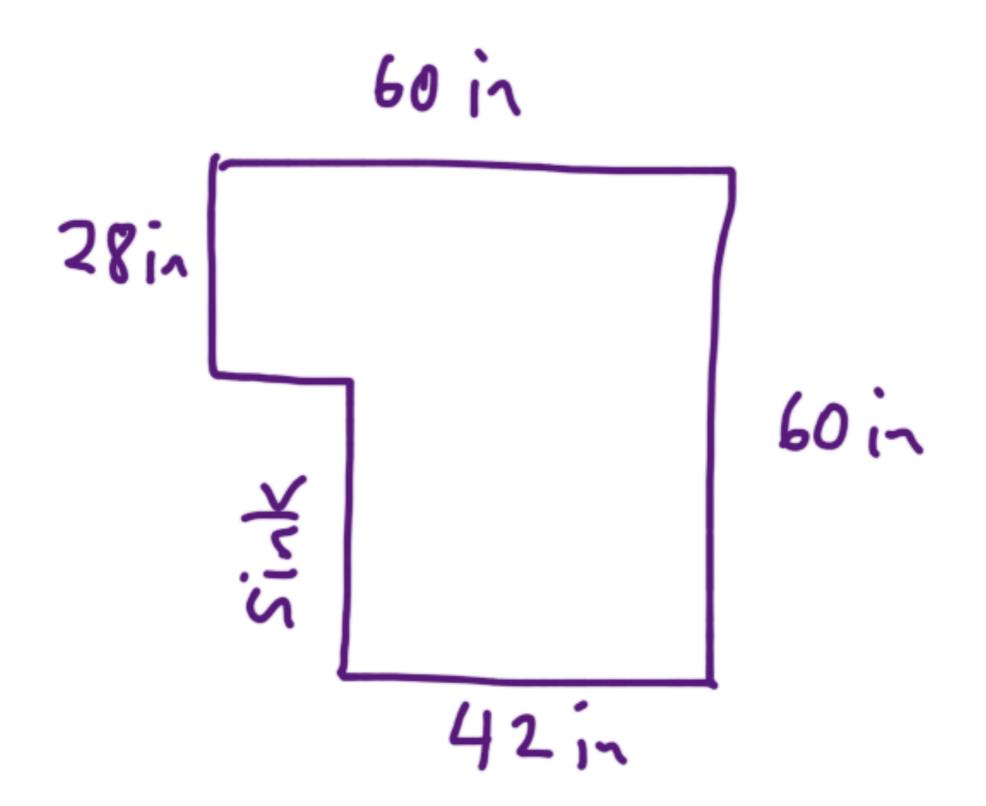
#### Teresa's Tiles

Teresa is going to put down new ceramic tiles on her bathroom floor. She has selected square tiles that are 4 inches on each side. These are the kind of tiles that can be placed right next to each other without leaving additional space for grout. At The Home Station, she learned how to cut the tiles in case she needs any fractional pieces to cover her floor completely.



This diagram of the bathroom floor shows the dimensions of the floor space she needs to cover. The sink area does not get tiled.

Questions: How many tiles will she need to buy to cover her floor? How many tiles will she have to cut in order to cover the entire space?



#### Teresa's Tiles "Scenario"

Things that some "low-performing" 8th graders noticed about the picture:

- two sides are equal
- two sides are 60 inches
- one side is 28 inches
- they are longest
- one side is 42 inches
- it used to be a square
- your lines aren't very straight
- the short side of the sink is 18"
- the sink is a rectangle
- the long side of the sink is 32"
- can find the area of the whole thing by making it two pieces

# There are 125 sheep and 5 dogs in a flock. How old is the shepherd?

Robert Kaplinsky (@robertkaplinsky) gave this to 32 eighth grade students. How many do you think attempted to find a numerical answer?

### How Old is the Shepherd?

75% gave numerical answers.

100% of his sixth graders gave numerical answers.

In the original research paper [Reusser 1986], "...three out of four school children will produce a numerical answer to this problem."

http://robertkaplinsky.com/how-old-is-the-shepherd/ https://www.youtube.com/watch?v=kibaFBgaPx4

#### Sample Grade 3 Test Question

The corner deli sells roses in bunches of 6. If Dylan buys 3 bunches of roses, how many roses does he have?

A.6 18%

B.9 46%

C.18 31%

D.24 4%

Combined scores of the 160 third graders in a group of four low-performing schools I used to support.

#### Sample Test Question Revised

The corner deli sells roses in bunches of 6. Dylan bought 3 bunches. Draw a picture of the story.



#### **CCSS Math Practice 1**

Make sense of problems and persevere in solving them.

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution.

They analyze givens, constraints, relationships, and goals.

They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt.

They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution.

They monitor and evaluate their progress and change course if necessary.

#### Sample Grade 3 Test Question

Hot dog buns come in packages of 8. Michael buys 6 packages of hot dog buns. How many hot dog buns does Michael have in all?

A.14 43%

B.36 **8%** 

C.48 40%

D.56 5%

## "Cracking the Math Code"

Λ			IT		NI	
A	U	U		U	IN	

**SUBTRACTION** 

MULTIPLICATION DIVISION

Add

Altogether

And

Both

How many

How much

In all

Increased by

Plus

Sum

Together

Total

are not

change

decreased by

difference

fewer

have left

how many did not

have

how many more

less than

remain

subtract

take away

Taller/shorter

By (dimension)

Double

Each group

Multiplied by

Of

Product of

Times

Triple

as much

cut up

divided by

each group has

half (or other

fractions)

how many in each

parts

quotient of

Separated

Share something

equally

split

(document from the web site of a large Eastern US metropolitan school district)

#### Sample Grade 3 Test Question

Hot dog buns come in packages of 8. Michael buys 6 packages of hot dog buns. How many hot dog buns does Michael have in all?

A.14 43%

B.36 **8%** 

C.48 40%

D.56 5%

#### Integrated Math 2 (Grade 10)

	Boy	Girl	Total
Wear Sunscreen	84	133	217
Do Not Wear Sunscreen	170	118	288
Total	254	251	505

P(wears sunscreen)

P(wears sunscreen and is a boy)

P(is a boy)

P(wears sunscreen *or* is a boy)

P(wears sunscreen | is a boy)

P(is a boy | wears sunscreen)

P(is a boy or a girl)

### "Doing Math" or Sense Making?

$$12 - p = 5$$

$$12 - ? = 5$$

[Michelle's son] was struggling to "remember" 28/4. When [she] asked him, "How do you think about 28/4?" He replied, "Mom, you aren't supposed to think about it, you are just supposed to do it!!"

#### Teacher Knows Best

$$\frac{3}{4} + \frac{5}{8} = \frac{8}{12}$$

## Student Perceptions of Math and Sense Making

- 1. You aren't supposed to sense-make when doing math.
- 2. You are supposed to use rules and algorithms and accept whatever answer results.
- 3. You are supposed to do what your teacher said, even when it doesn't seem like a good idea.

## The Five Strands of Mathematical Proficiency

National Research Council, 2001, Adding it up: Helping children learn mathematics.

- 1. Conceptual understanding
- 2. Procedural fluency
- 3. Strategic competence
- 4. Adaptive reasoning
- 5. Productive disposition

"Productive disposition is the inclination to see mathematics as sensible, useful, and worthwhile, coupled with a belief in diligence and one's own efficacy."

## Characteristics of Strong Readers Mathematicians

- They are motivated to read. tackle problems
- They are able to read words accurately and automatically.
- They comprehend what they read.
- They are able to read with expression.
- They use a variety of strategies to tackle words they don't recognize.
- They use active problem solving strategies to search for information, to determine meaning, to make sense of words, to make connections.

## Encouraging Sense Making

Q: What's one way to cultivate a classroom focused on sense making rather than answer-getting?

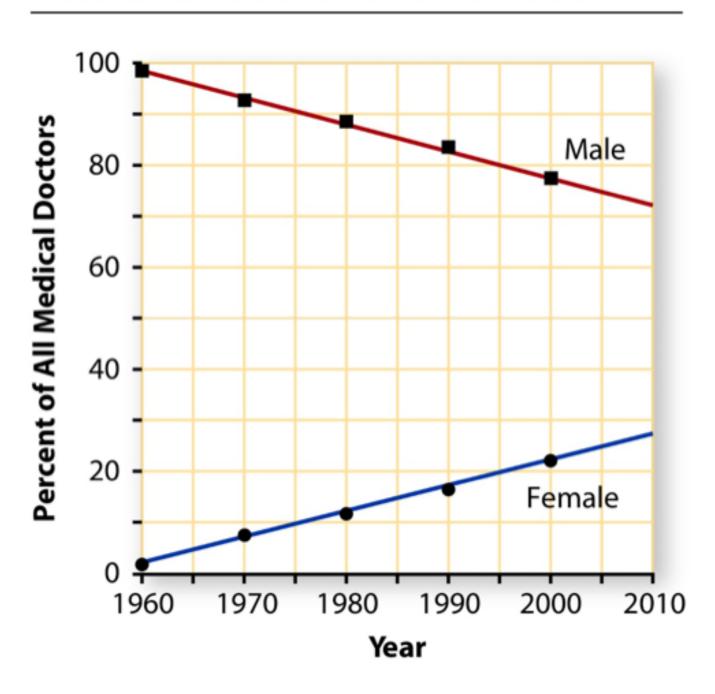
A: Get rid of the question. Literally.

Apple juice costs 50¢. The juice machine accepts quarters, dimes, and nickels.

1 Wonder		

Mr. Gavin has a ladder that is 100 centimeters tall.
Ms. Cornell has a ladder that is 2 meters tall.

#### Male and Female Medical Doctors



#### The No-ID Voter

23



28



The Procrastinating Voter

34

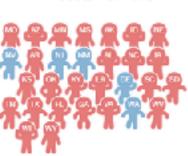


17



The Convicted-Felon Voter

30



21

COULD VOTE



#### The Working-Parent Voter

27



24

COULD YOTE



What's Going On in This Graph?

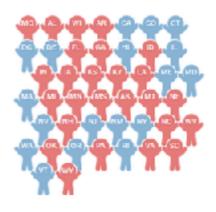
NY Times
Learning Network
#NYTGraphChat

The Eager Student Voter

7



44



Every Wednesday!

- States with a Republican majority in the state House of Representatives
- States with a Democratic majority in the state House of Representatives

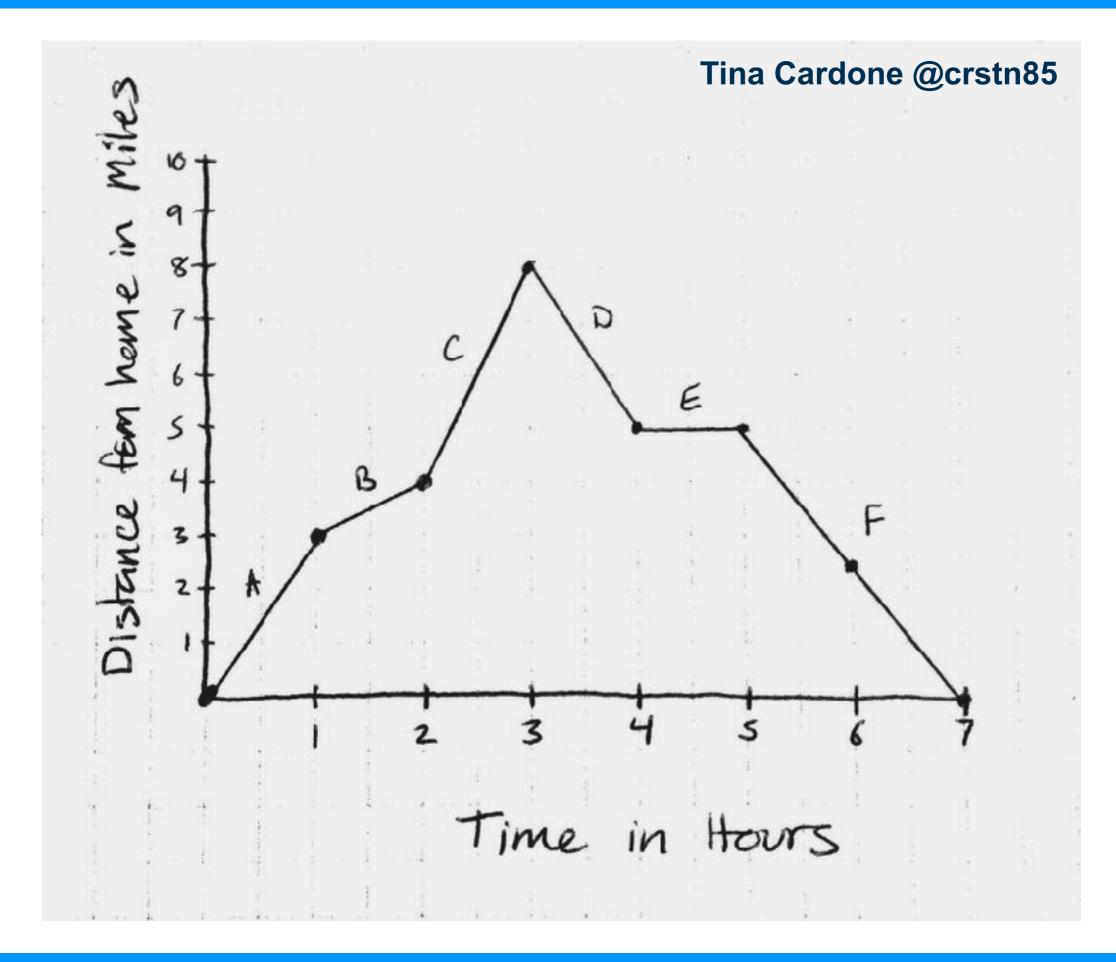
After looking closely at the infographic above, think about these three questions:

- What do you notice?
- What do you wonder?

What are you curious about that comes from what you notice in the infographic?

What might be going on in this infographic?

Write a catchy headline that captures the infographic's main idea. If your headline makes a claim, tell us what you noticed that supports your claim.





#### Tina Cardone @crstn85 · Nov 24

@MFAnnie when I gave the graph and did notice/wonder first I didn't have to answer nearly so many questions when they did the handout











#### Tina Cardone @crstn85 · Nov 24

@MFAnnie worth the few minutes it took and meant we skipped wrap up discussion (they already had it) drawingonmath.blogspot.com/2014/11/distan...









http://drawingonmath.blogspot.com/2014/11/distance-graph.html

### Encouraging Sense-Making

Q: What's another way to cultivate a classroom focused on sense making rather than answer-getting?

A: Get rid of the question *and* the numbers.

## Get Rid of the Question and the Numbers

Raul had some pet mice. Xavier gave him some more mice.

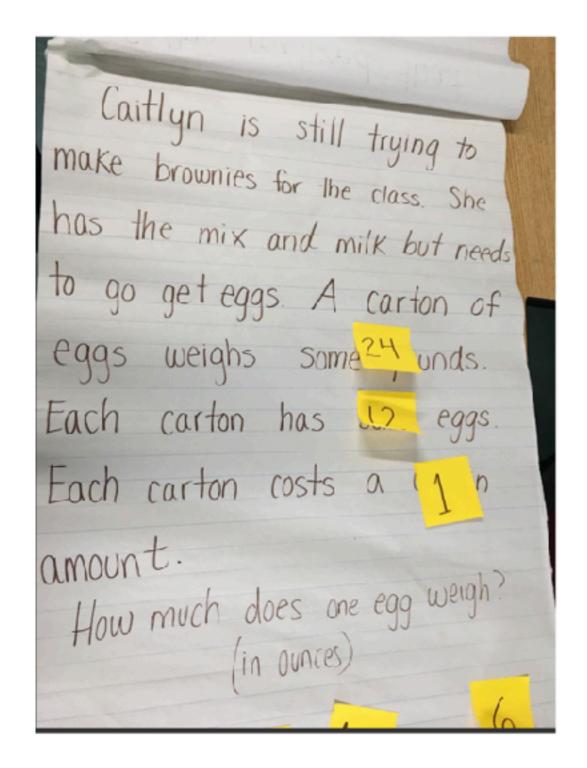
Raul had some pet mice. Xavier gave him 3 more mice.

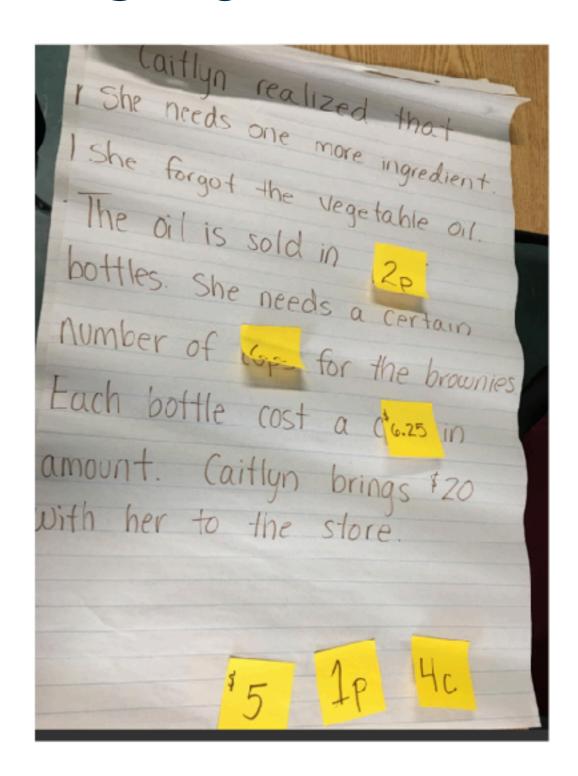
Raul had some pet mice. Xavier gave him 3 more mice. Now Raul has 8 mice.

Raul had some pet mice. Xavier gave him 3 more mice. Now Raul has 8 mice. How many mice did Raul have to start with?

A Numberless Word Problem from Brian Bushart, bstockus.wordpress.com

#### Give the Answer

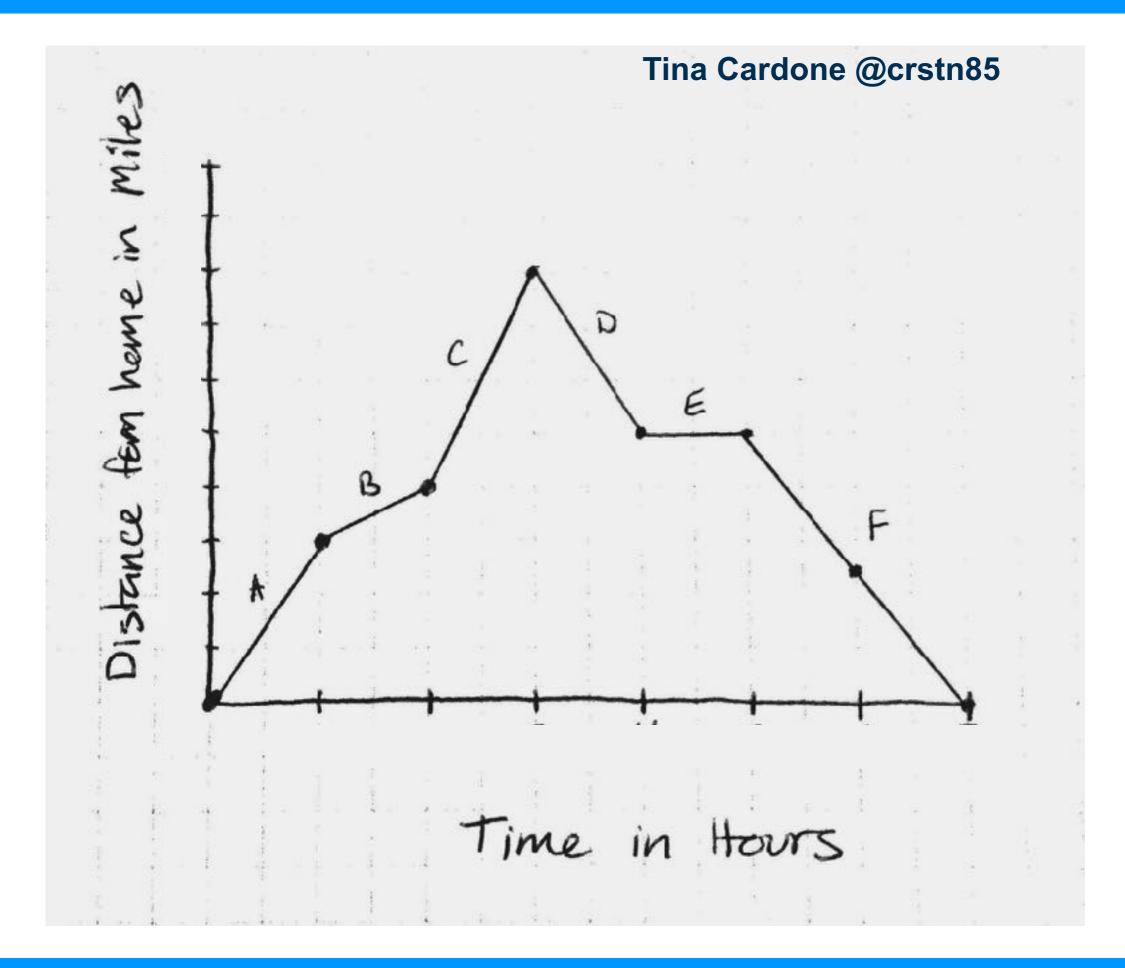




From Kat Kulis, grade 5, Windham Center School, Windham, CT

## Get Rid of the Question and the Numbers

A store has the floor Women's plan shown. The area of the women's Girls' department is Sporting Goods Men's



### Numbers vs. Relationships

### Encouraging Sense Making

Q: What's another way to cultivate a classroom focused on sense making rather than answer-getting?

A: Give the answer.

#### Give the Answer

#### ◆ Math Message Follow-Up

#### WHOLE-CLASS ACTIVITY

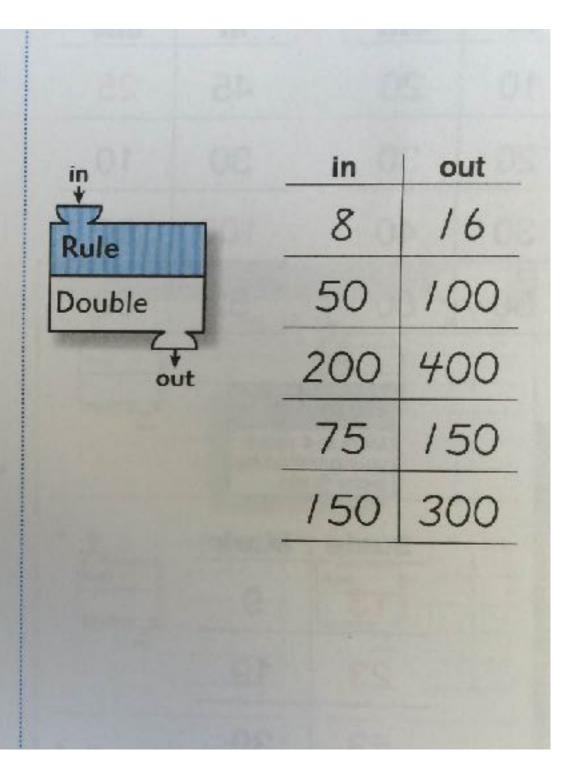
Draw or display a function machine and "What's My Rule?" table. (See Advance Preparation.)

Ask children to imagine that the function machine works like this:

- · A number (the input) is dropped into the machine,
- the machine changes the number according to a rule,
- and a new number (the output) comes out the other end.

The **rule** for the Math Message problem is "Double the number." Write the word *Double* in the function machine.

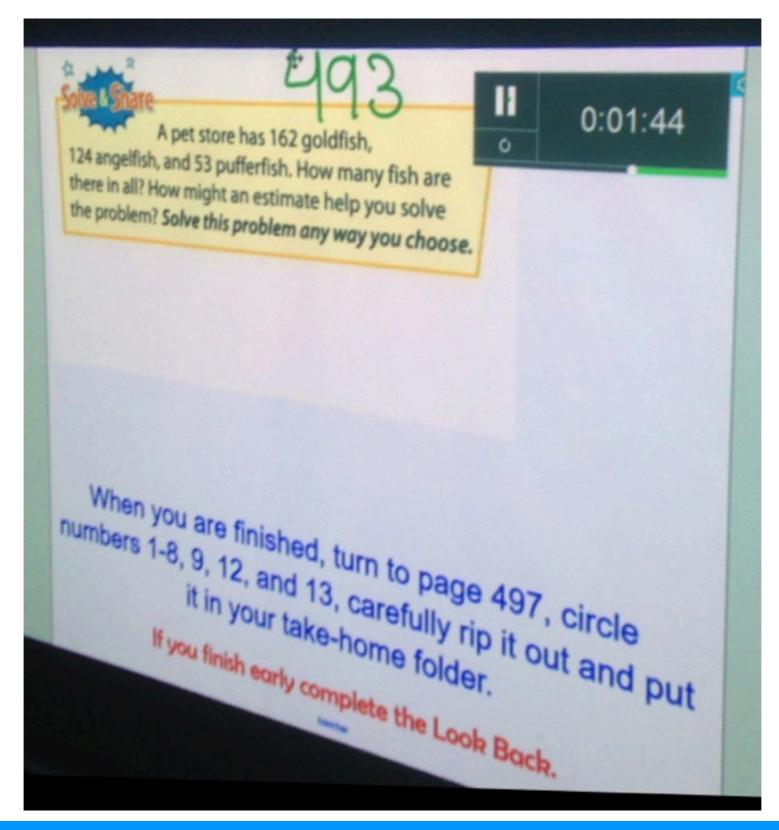
Point out the "What's My Rule?" table. Discuss the 8 in the *in* column and the 16 in the *out* column. Explain to children that numbers in the *in* column represent the numbers of bacteria now. Corresponding numbers in the *out* column represent the numbers of bacteria 20 minutes from now.



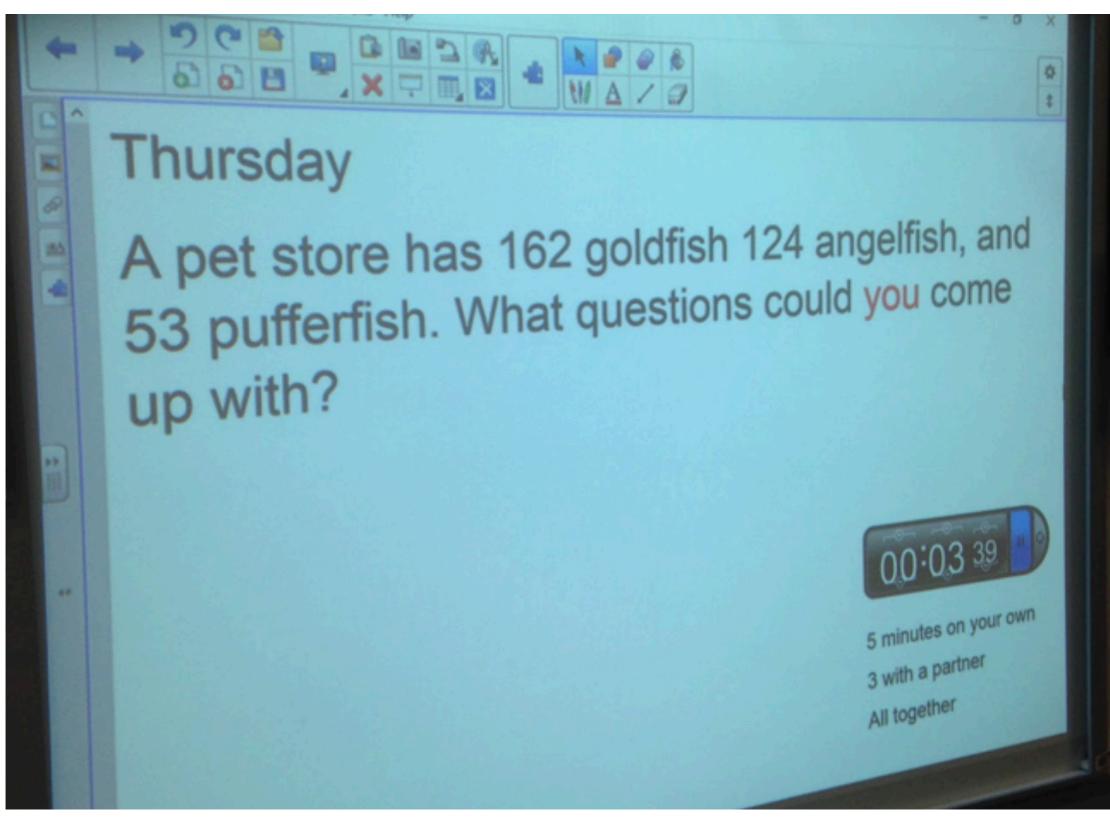
#### Give the Answer

in	in	out
Rule	8	16
Double	50	100
out	200	400
	75	150
	150	300

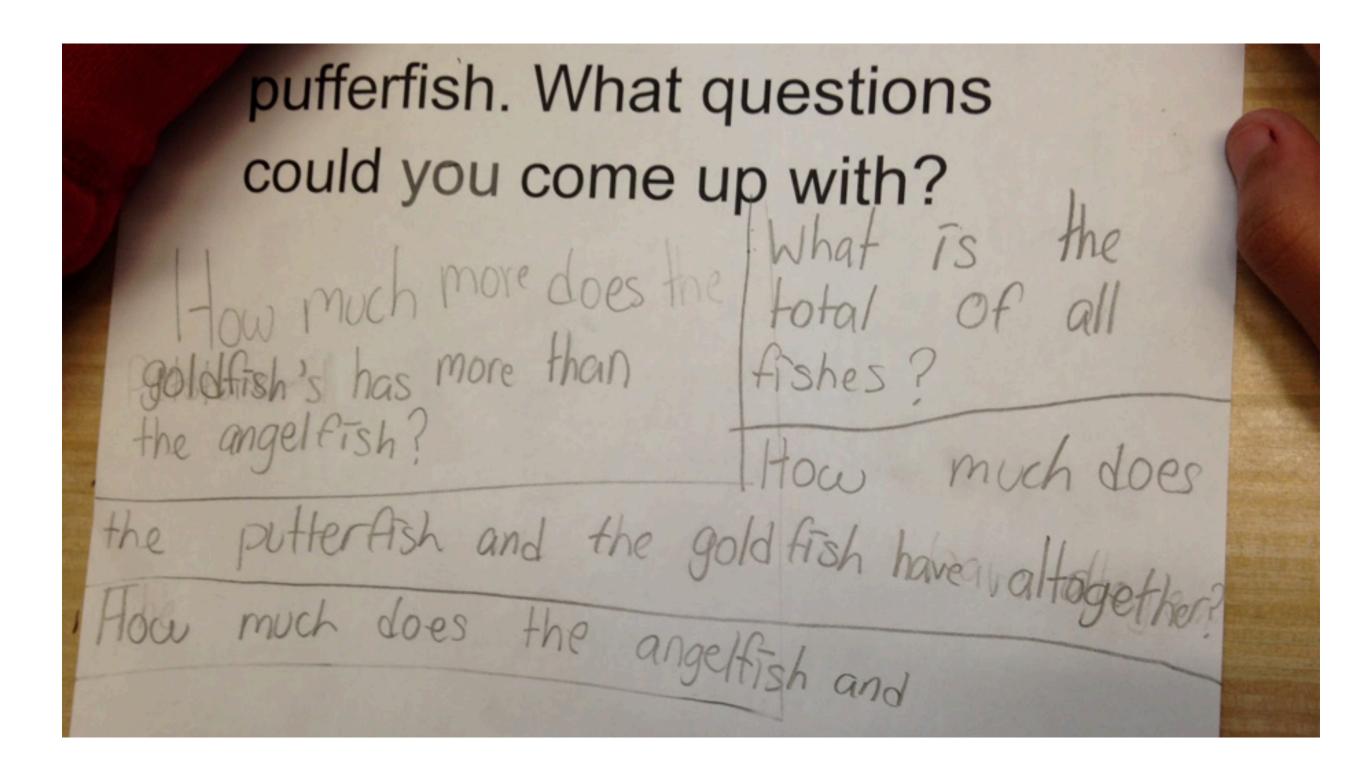
#### Variation: Ask for Questions



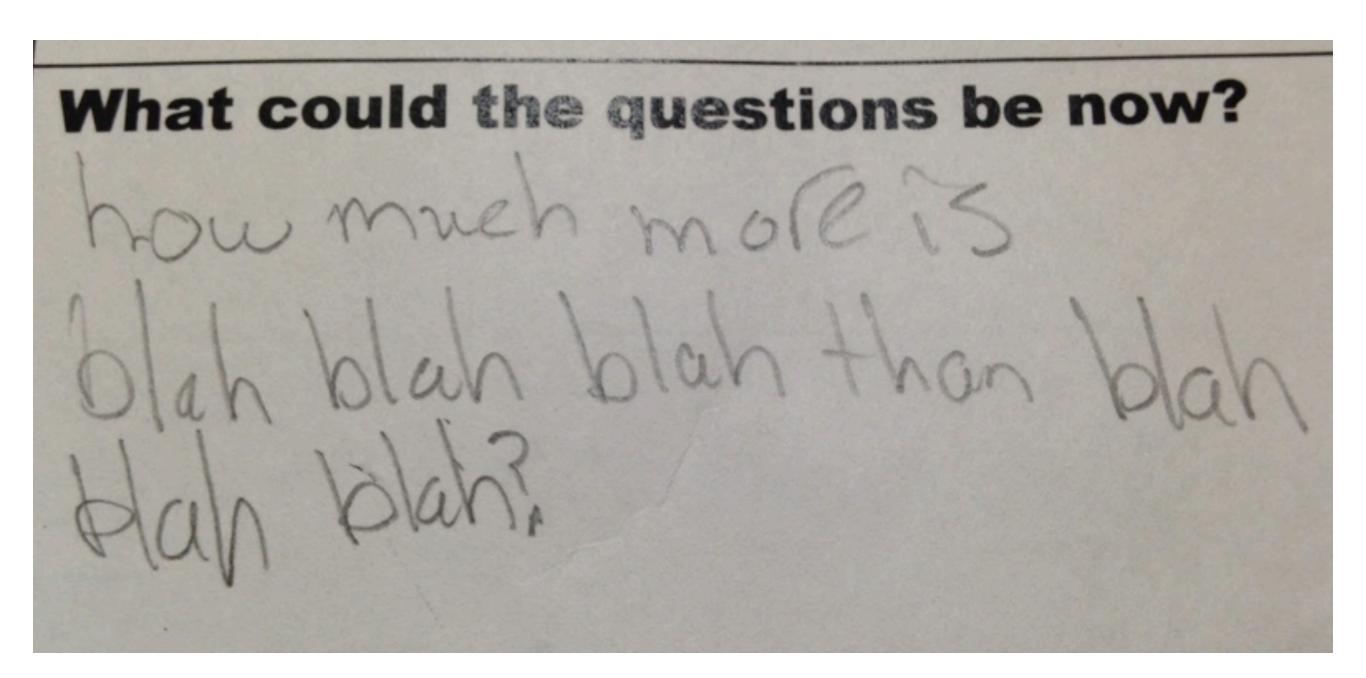
#### Variation: Ask for Questions



#### Variation: Ask for Questions



#### Variation: Ask for Questions



#### Give the Answer (or Several!)

Rachel bakes cookies and delivers them to her friends.

- It takes 8 minutes to mix the batter.
- The cookies bake for 9 minutes.
- For 6 minutes they cool.

If the answer is 23 minutes, what is the question? If the answer is 3 minutes, what is the question? If the answer is bake, what is the question?

from Joe Schwartz, @JSchwartz10a

### Encouraging Sense Making

Q: What's another way to cultivate a classroom focused on sense making rather than answergetting?

A: Ask about ideas, not answers.

This can be really simple:

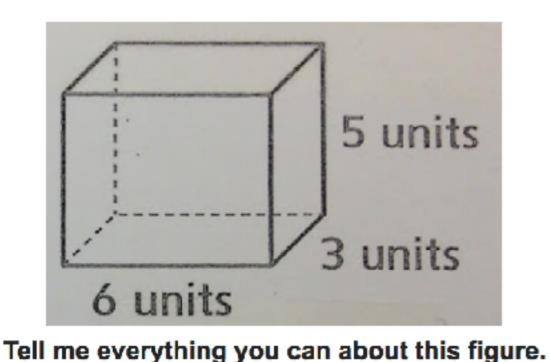
"Tell me something about number 7."

instead of

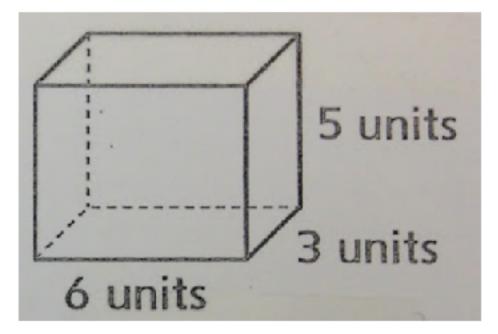
"What's the answer to number 7?"

#### Ask About Ideas, Not Answers

It can be a little more complex:



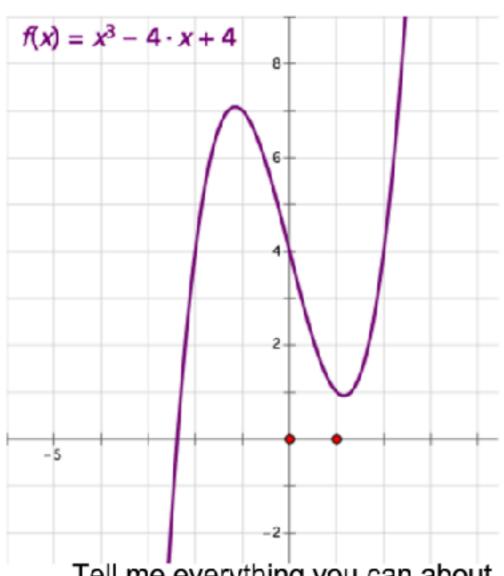
instead of



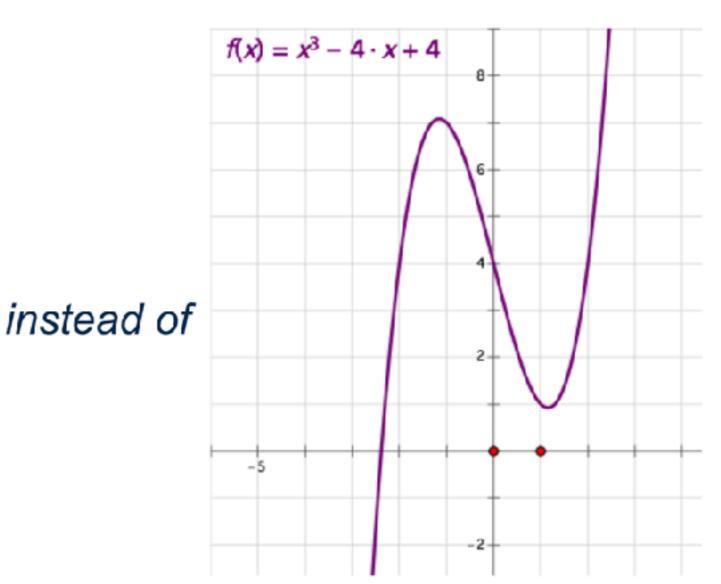
Find the volume of the rectangular prism.

(from Joe Schwartz's blog, exit10a.blogspot.com, October 10, 2016)

#### Ask About Ideas, Not Answers

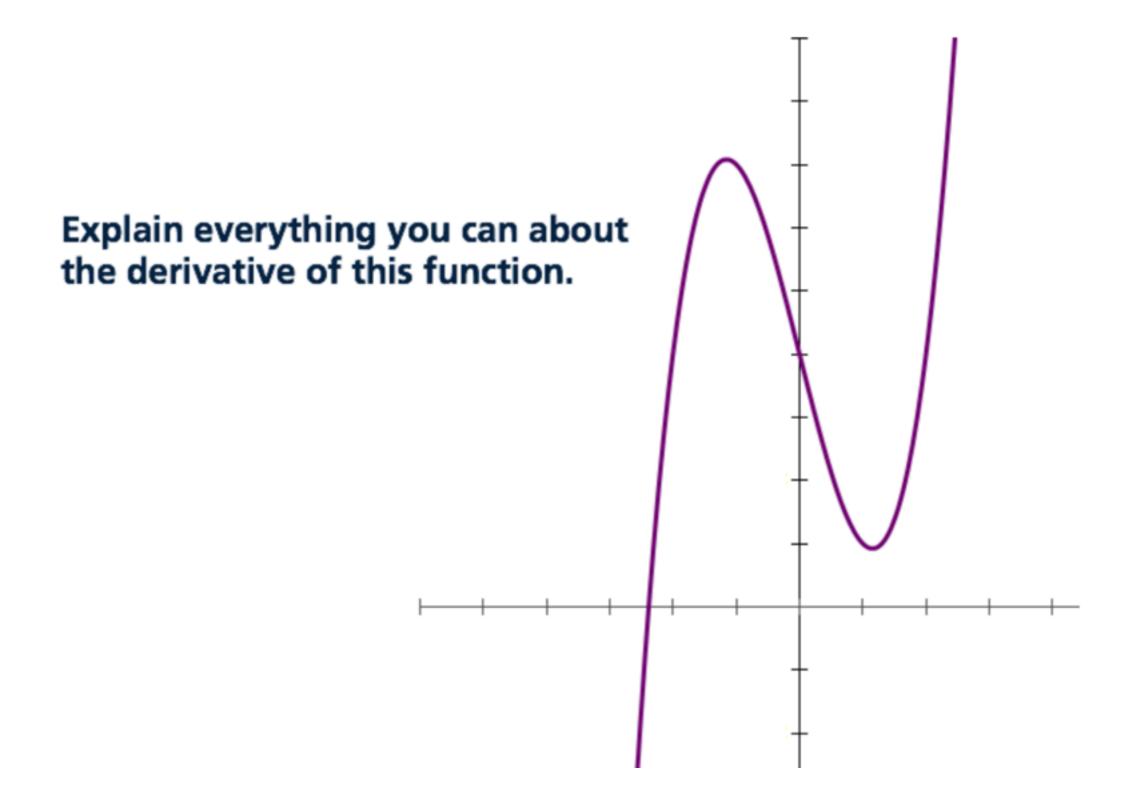


Tell me everything you can about the derivative of this function.



Find the derivative of this function.

#### Ask About Ideas, Not Answers



#### Teacher Questions

"Why?"

"How do you know?"

"How did you decide?"

"Tell me more about that."

#### "Phone in Pocket"

Are you asking *idea-focused* questions or answer-focused questions? Record yourself and find out!

**#ToVForRatio** 

# Ways to Encourage Sense Making Rather Than Answer Getting

- Get rid of the question.
- Get rid of the question and the numbers.
- Give the answer.
- Ask about ideas, not answers.

#### Personal Reflection

Write down two things you noticed in this session and two things you are wondering.

#### Mingle Instructions

- Stand up and move around.
- Find someone and introduce yourself.
- Ask them one question from the list.
- Listen to their answer.
- Move on to find another person.
- No back and forth, just ask one question and listen to the answer.
- When I raise my hand, finish your conversation and raise your hand.

## Thank you!

#### **Annie Fetter**

anniefetter@gmail.com, @MFAnnie

Slides and links to related resources will be available on my blog after the talk:

annie.mathematicalthinking.org